



# RAMA UNIVERSITY

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## FACULTY OF ENGINEERING

### Digital Image Processing LECTURE-23

**Mr. Dharendra**

Assistant Professor

Computer Science & Engineering

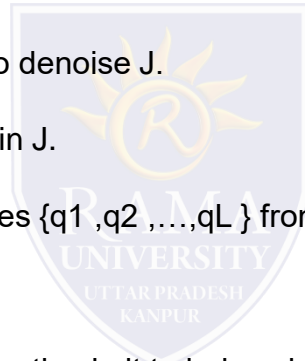
# OUTLINE

- ❖ Use of PCA for denoising
- ❖ Patch similarity
- ❖ MCQ
- ❖ References



# Use of PCA for denoising

- This “non-local” principle can be combined with PCA for denoising.
- Consider a clean image  $I$  corrupted by additive Gaussian noise of mean zero and standard deviation  $\sigma$ , to give noisy image  $J$  as follows:  $J = I + N$ ,  $N \sim$  Gaussian distribution of mean 0 and standard deviation  $\sigma$ .
- Given  $J$ , we want to estimate  $I$ , i.e. we want to denoise  $J$ .
- Consider a small  $p \times p$  patch – denoted  $q_{ref}$  - in  $J$ .
- Step 1: We will collect together some  $L$  patches  $\{q_1, q_2, \dots, q_L\}$  from  $J$  that are structurally similar to  $q_{ref}$  – pick the  $L$  nearest neighbors of  $q_{ref}$ .
- Note: even if  $J$  is noisy, there is enough information in it to judge similarity if we assume  $\sigma \ll$  average intensity of the true image  $I$ .
- Step 2: Assemble these  $L$  patches into a matrix of size  $p^2 \times L$ . Let us denote this matrix as  $X_{ref}$



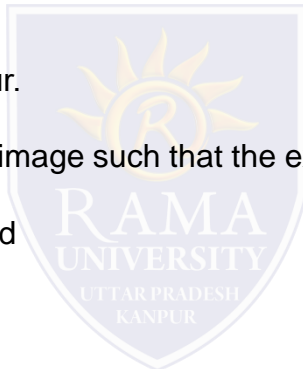
# Use of PCA for denoising

Spread spectrum filters are not always possible in many applications.

- The inverse filter approach on previous slides made no explicit use of the knowledge of the noise model.
- The Wiener filter is one approach which makes use of knowledge of the statistical properties of the noise besides the degradation function.

- It attempts to remove both noise as well as the blur.

- Its aim is to produce an estimate of the underlying image such that the expected mean square error between the true and estimated images is minimized



# Use of PCA for denoising

Consider a small  $p \times p$  patch – denoted  $q_{ref}$  - in  $J$ .

- **Step 1:** We will collect together some  $L$  patches  $\{q_1, q_2, \dots, q_L\}$  from  $J$  that are structurally similar to  $q_{ref}$  – pick the  $L$  nearest neighbors of  $q_{ref}$ .

- Note: even if  $J$  is noisy, there is enough information in it to judge similarity if we assume  $\sigma \ll$  average intensity of the true image  $I$ .

- **Step 2:** Assemble these  $L$  patches into a matrix of size  $p \times L$ . Let us denote this matrix as  $X_{ref}$ .

**Step 3:** Find the eigenvectors of  $X_{ref} X_{ref}^T$  to produce an eigenvector matrix  $V$ .

- **Step 4:** Project each of the (noisy) patches  $\{q_1, q_2, \dots, q_L\}$  onto  $V$  and compute their eigencoeficient vectors denoted as  $\{\alpha_1, \alpha_2, \dots, \alpha_L\}$  where  $\alpha_i = V^T q_i$ .

- **Step 5:** Now, we need to manipulate the eigencoeficients of  $q_{ref}$  in order to denoise it.

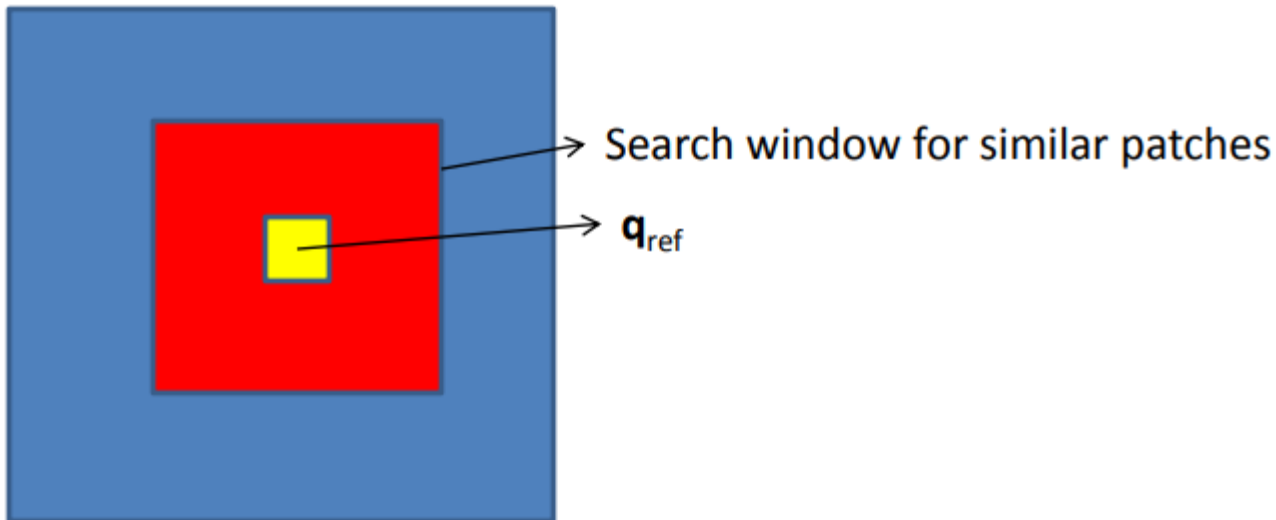
# Patch similarity: Use of PCA for denoising

To compute L nearest neighbors of  $q_{ref}$ , restrict your search to a window around  $q_{ref}$ .

- For every patch within the window, compute the sum of squared differences with  $q_{ref}$ , i.e. compute: .

$$\sum_{i=1}^P \sum_{j=1}^P (q_{ref}(i, j) - s(i, j))^2$$

- Pick L patches with the least distance



1. The objective of sharpening spatial filters is/are to \_\_\_\_\_
  - a) Highlight fine detail in an image
  - b) Enhance detail that has been blurred because of some error
  - c) Enhance detail that has been blurred because of some natural effect of some method of image acquisition
  - d) All of the mentioned
2. Sharpening is analogous to which of the following operations?
  - a) To spatial integration
  - b) To spatial differentiation
  - c) All of the mentioned
  - d) None of the mentioned
3. Which of the following fact(s) is/are true about sharpening spatial filters using digital differentiation?
  - a) Sharpening spatial filter response is proportional to the discontinuity of the image at the point where the derivative operation is applied
  - b) Sharpening spatial filters enhances edges and discontinuities like noise
  - c) Sharpening spatial filters deemphasizes areas that have slowly varying gray-level values
  - d) All of the mentioned

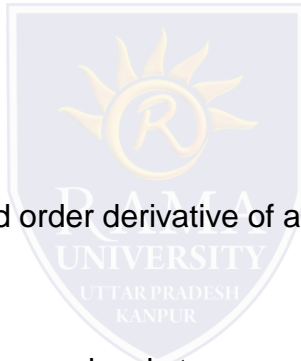


4. Which of the facts(s) is/are true for the first order derivative of a digital function?

- a) Must be nonzero in the areas of constant grey values
- b) Must be zero at the onset of a gray-level step or ramp discontinuities
- c) Must be nonzero along the gray-level ramps
- d) None of the mentioned

5. Which of the facts(s) is/are true for the second order derivative of a digital function?

- a) Must be zero in the flat areas
- b) Must be nonzero at the onset and end of a gray-level step or ramp discontinuities
- c) Must be zero along the ramps of constant slope
- d) All of the mentioned





# References

- <https://www.javatpoint.com/digital-image-processing-tutorial>
- <https://www.geeksforgeeks.org/>
- Digital Image Processing 2nd Edition, Rafael C. Gonzalvez and Richard E. Woods. Published by: Pearson Education.
- Digital Image Processing and Computer Vision, R.J. Schalkoff. Published by: JohnWiley and Sons, NY.
- Fundamentals of Digital Image Processing, A.K. Jain. Published by Prentice Hall,Upper Saddle River, NJ.

