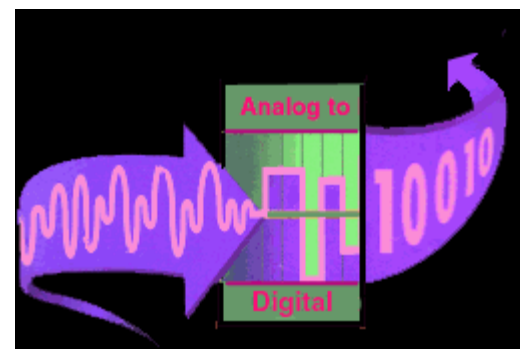




FACULTY OF ENGINEERING & TECHNOLOGY

- Analog signals are continuous, with infinite values in a given range.
- Digital signals have discrete values such as on/off or 0/1.
- Limitations of analog signals
 - Analog signals pick up noise as they are being amplified.
 - Analog signals are difficult to store.
 - Analog systems are more expensive in relation to digital systems.

- Advantages of digital systems (signals)
 - Noise can be reduced by converting analog signals in 0s and 1s.
 - Binary signals of 0s/1s can be easily stored in memory.
 - Technology for fabricating digital systems has become so advanced that they can be produced at low cost.
- The major limitation of a digital system is how accurately it represents the analog signals after conversion.



Embedded System

- A typical system that converts signals from analog to digital and back to analog includes:
 - A transducer that converts non-electrical signals into electrical signals
 - An A/D converter that converts analog signals into digital signals
 - A digital processor that processes digital data (signals)
 - A D/A converter that converts digital signals into equivalent analog signals
 - A transducer that converts electrical signals into real life non-electrical signals (sound, pressure, and video)

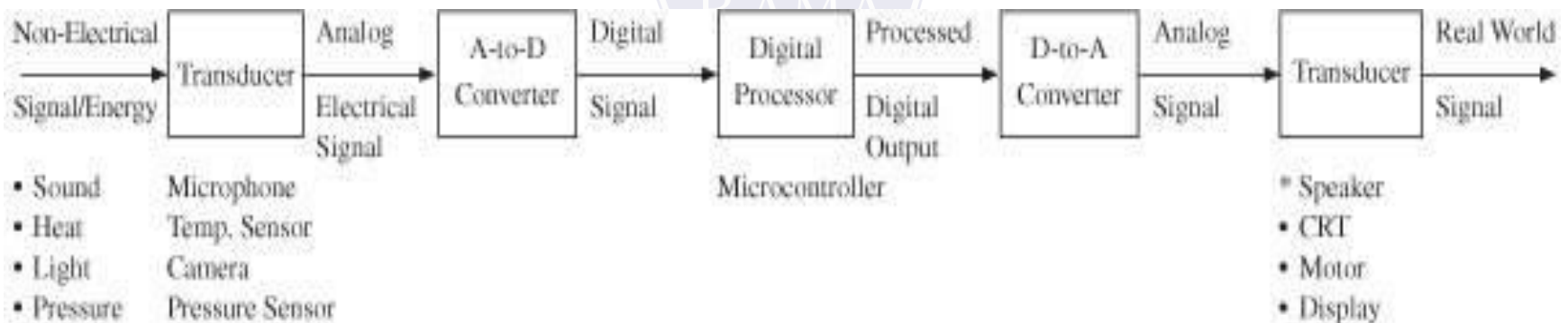
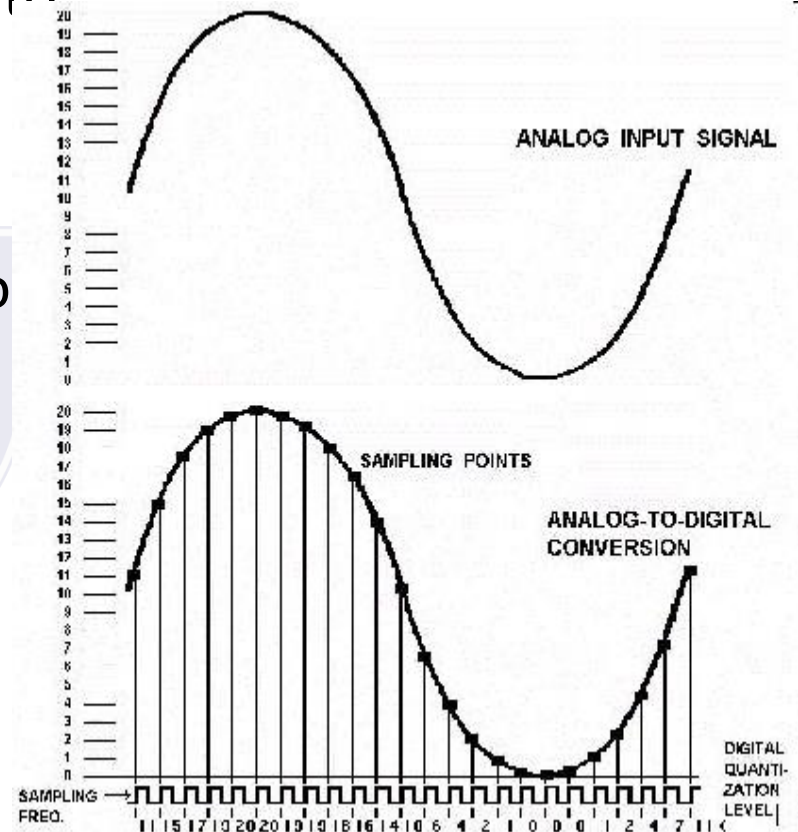


FIGURE 12-1 Embedded Systems: A-to-D and D-to-A Signal Conversion

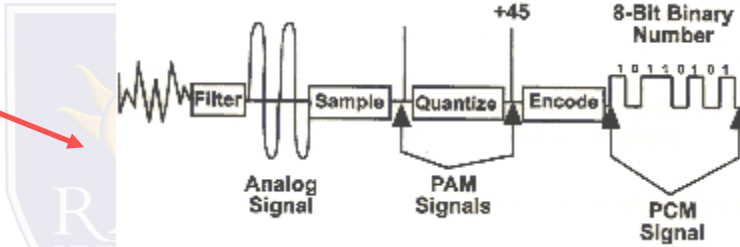
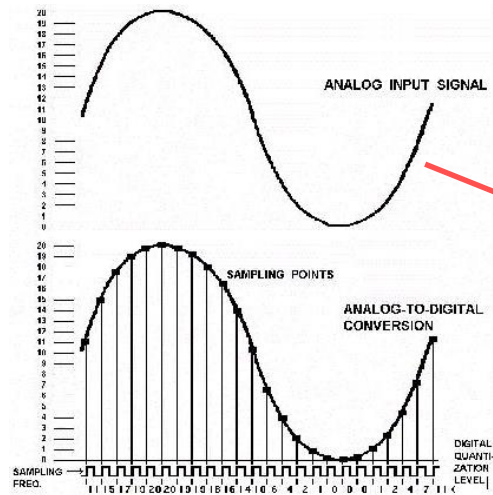
So, how does A/D Converter works?

A/D Converter

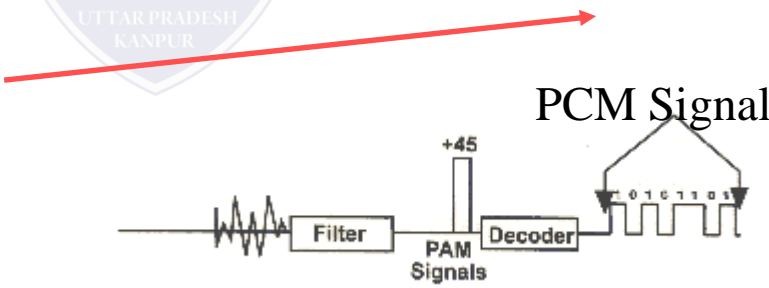
- In order to change an analog signal to digital, the input analog signal is **sampled** at a high rate of speed.
- The amplitude at each of those sampled moments is converted into number equivalent – this is called **quantization**.
- These numbers are simply the combinations of the 0s and 1s used in computer language – this called **encoding**.



A/D Conversion – Pulse Code Modulation/Demodulation

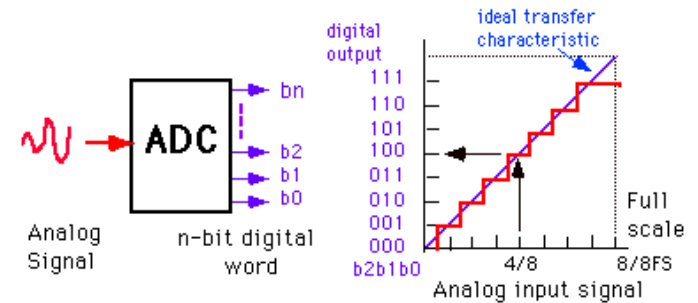


Modulation



Demodulation

Analog-to-Digital



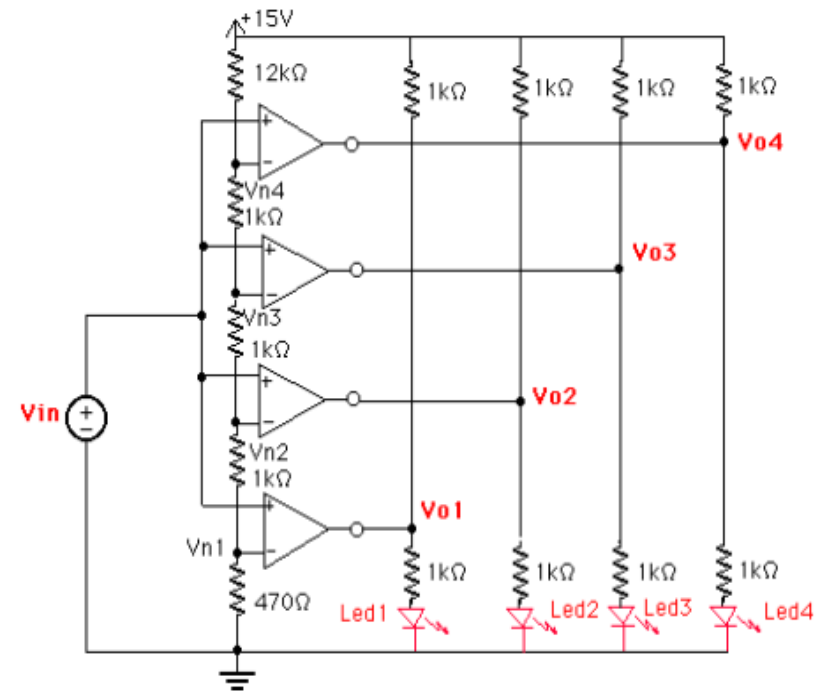
- A simple hypothetical A/D converter circuit with one analog input signal and three digital output lines with eight possible binary combinations: 000 to 111
 - Shows the graph of digital output for FS V analog input
- The following points can be summarized in the above process:
 - **Maximum value** this quantization process reaches is $7/8$ V for a 1 V analog signal; includes $1/8$ V an inherent error
 - $1/8$ V (an inherent error) is also equal to the value of the Least Significant Bit (**LSB**) = 001.
 - **Resolution** of a converter is defined in terms of the number of discrete values it can produce; also expressed in the number of bits used for conversion or as $1/2^n$ where n = number of bits
 - The value of the most significant bit (**MSB**) -100- is equal to $1/2$ the voltage of the full-scale value of 1 V.
 - The value of the **largest digital number** 111 is equal to full-scale value minus the value of the LSB.
 - The **quantization error** can be reduced or the resolution can be improved by increasing the number of bits used for the conversion

A/D Conversion - Types

- Can be classified in four groups:
 - **Integrator:**
 - Charges a capacitor for a given amount of time using the analog signal.
 - It discharges back to zero with a known voltage and the counter provides the value of the unknown signal.
 - Provides slow conversion but low noise.
 - Often used in monitoring devices (e.g., voltmeters)
 - **Flash:** uses multiple comparators in parallel.
 - The known signal is connected to one side of the comparator and the analog signal to be converted to the other side of the comparator.
 - The output of the comparators provides the digital value.
 - This is a high-speed, high cost converter.

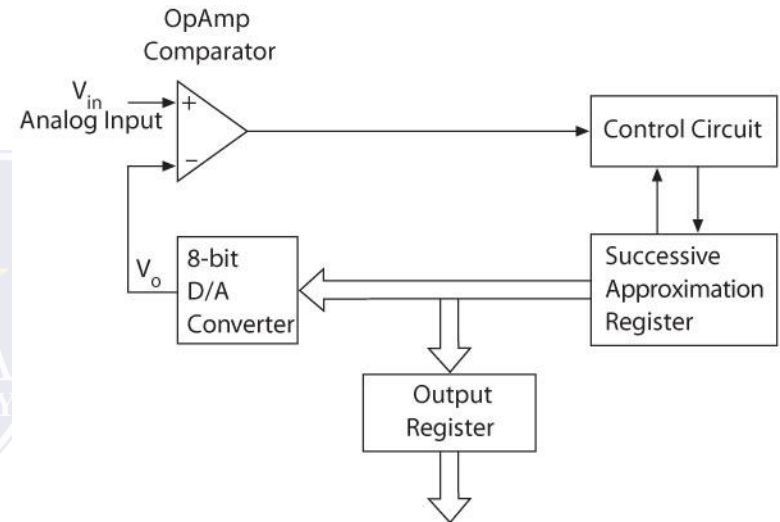
A/D Conversion

- Flash Converter
 - The circuit consists of 4 comparators whose inverting inputs are connected to a voltage divider.
 - A comparator is basically an operational amplifier used without feedback.
 - The outputs of the comparators correspond to a digital word.
 - When the input rises above V_{n1} , the first comparator will switch to a high output voltage causing the LED to light up, indicating a (0001).
 - For larger input voltages the output of other comparators will switch high as well. For large input voltages (above V_{n3}) all comparators will be high corresponding to (1111) digital output.



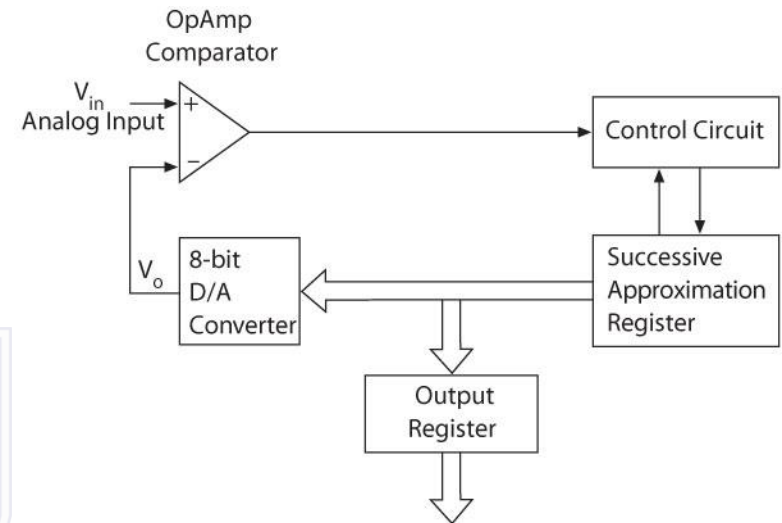
A/D Conversion

- **Successive approximation:** Includes a D/A (digital to analog) converter and a comparator. An internal analog signal is generated by turning on successive bits in the D/A converter.
- **Counter:** Similar to a successive approximation converter except that the internal analog signal is generated by a counter starting at zero and feeding it to the D/A converter.



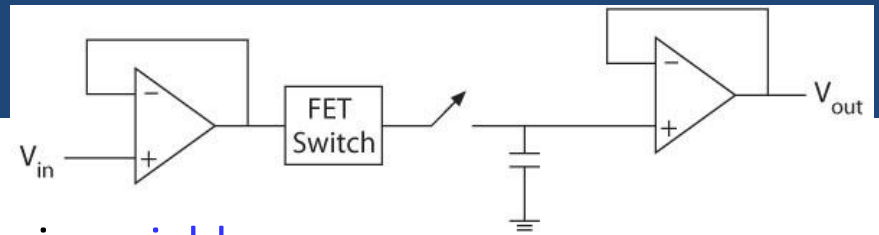
Successive Approximation A/D Converter Circuit

- The SAR (successive approximation register) begins by turning on the MSB Bit7.
- V_o of the D/A converter is compared with the analog input voltage V_{in} in the comparator.
- If analog voltage is less than the digital voltage, Bit7 is turned off and Bit6 is turned on.
- If analog voltage is greater than the digital voltage, Bit7 is kept on and Bit6 is turned on.
- The process of turning bit on/off is continued until Bit0.
- Now the 8-bit input to the D/A converter represents the digital equivalent of the analog signal V_{in} .



Bit 7 is set: $b_7=1$
If $V_a < V_d \rightarrow b_7=0; b_6=1$
If $V_a > V_d \rightarrow b_7=1; b_6=1$
.....
If $V_a < V_d \rightarrow b_7=0; \dots b_0=1$
If $V_a > V_d \rightarrow b_7=1; \dots b_0=1$
Done

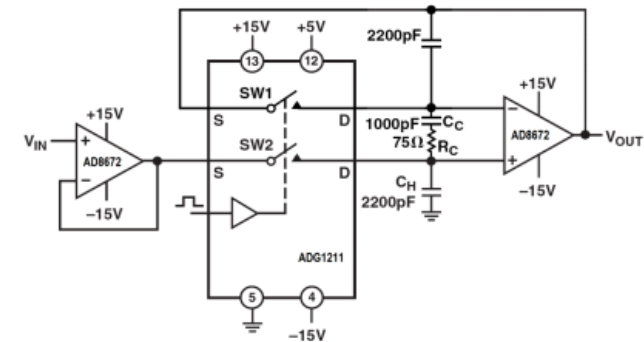
Sample and Hold Circuit



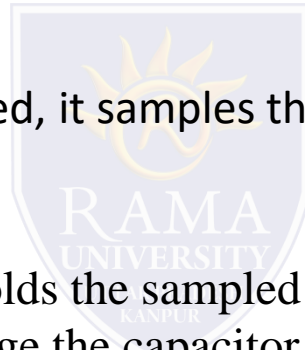
- If the input voltage to an A/D converter is **variable**, the digital output is likely to be unreliable and unstable. Therefore, the varying voltage source is connected to the ADC through a **sample and hold circuit**.

- **Basic Operation:**

- When the switch is connected, it samples the input voltage.



- When the switch is **open**, it holds the sampled voltage by **charging** the capacitor.
- **Acquisition time**: time to charge the capacitor **after the switch is open** and settle the output.
- **Conversion time**: total time needed from the start of a conversion (turning on the MSB in the SAR) until the end of the conversion (turning on/off Bit0 in the SAR)
 - **TAD**: conversion time per bit.



- Example 1
 - Assumes the input analog voltage is changing between 0-5 V.
 - Using a 3-bit A/D converter draw the output as the input signal ramps from 0 to 5V.
 - Calculate the resolution.
 - What is the maximum possible voltage out? (this is called the full-scale output)
 - If the output is 1000 0000, what is the input?
- Example 2
 - Assumes the input analog voltage is changing between -5 to 5 V; using a 10-bit A/D converter.
 - Calculate the number of quantization levels.
 - Calculate the voltage resolution.

- Example 1

- Assumes the input analog voltage is changing between 0-5 V.
- Using a 3-bit A/D converter draw the output as the input signal ramps from 0 to 5V.
- Calculate the resolution. $1 / 2^8 = 19.53 \text{ mV}$
- What is the maximum possible voltage out? (this is called the full-scale output) **5- Resolution**
- If the output is 1000 0000, what is the input? $\text{MaxVolt} / 2 = 2.5$

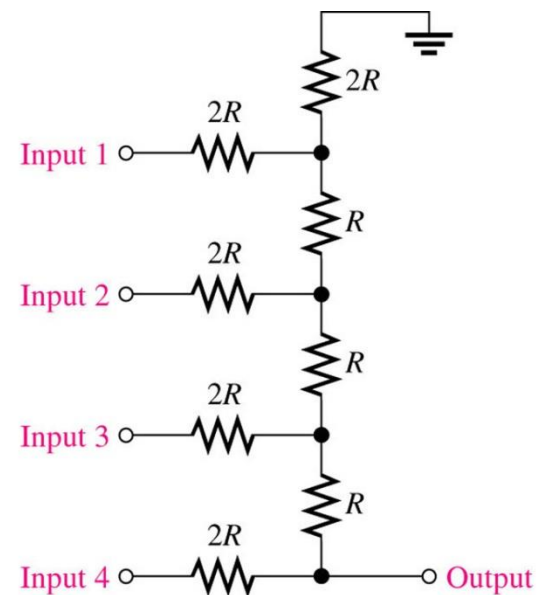
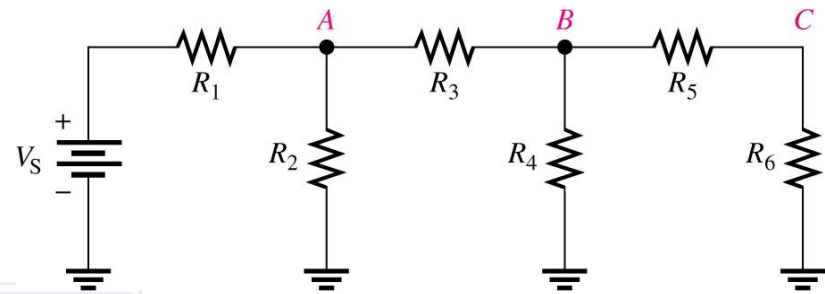
- Example 2

- Assumes the input analog voltage is changing between -5 to 5 V; using a 10-bit A/D converter.
- Calculate the number of quantization levels. 2^{10}
- Calculate the voltage resolution. $5 - (-5) / 1024 = 9.76 \text{ mV}$

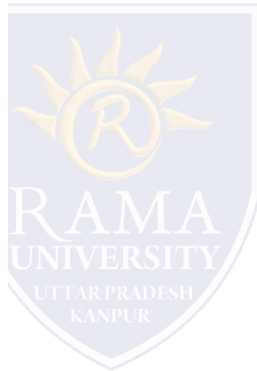
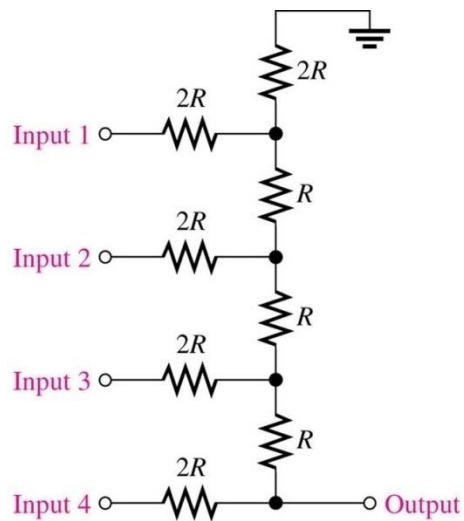
- Converting discrete signals into discrete analog values that represent the magnitude of the input signal compared to a standard or reference voltage
 - The output of the DAC is discrete analog steps.
 - By increasing the resolution (number of bits), the step size is reduced, and the output approximates a continuous analog signal.

Analysis of a Ladder Network

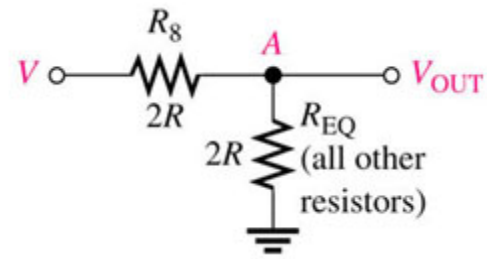
- A resistive ladder network is a special type of series-parallel circuit.
- One form of ladder network is commonly used to **scale down voltages** to certain weighted values for digital-to-analog conversion
 - Called **R/2R Ladder Network**
- To find total resistance of a ladder network, start at the **point farthest** from the source and reduce the resistance in steps.



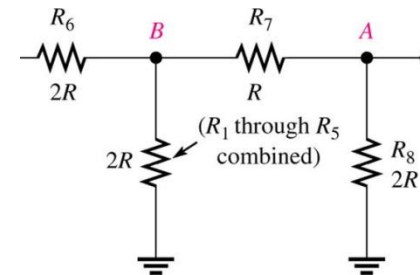
The R/R2 Ladder Network



Only Input 4 is HIGH



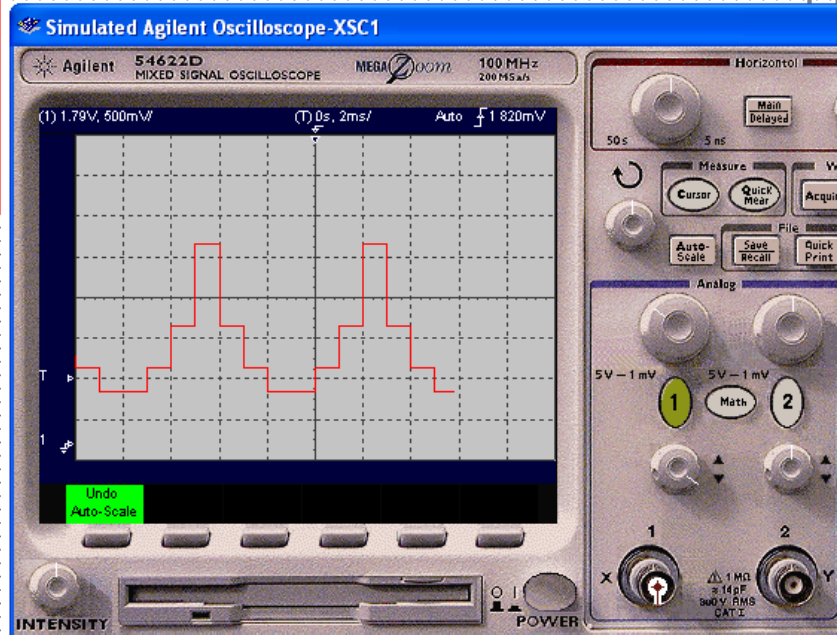
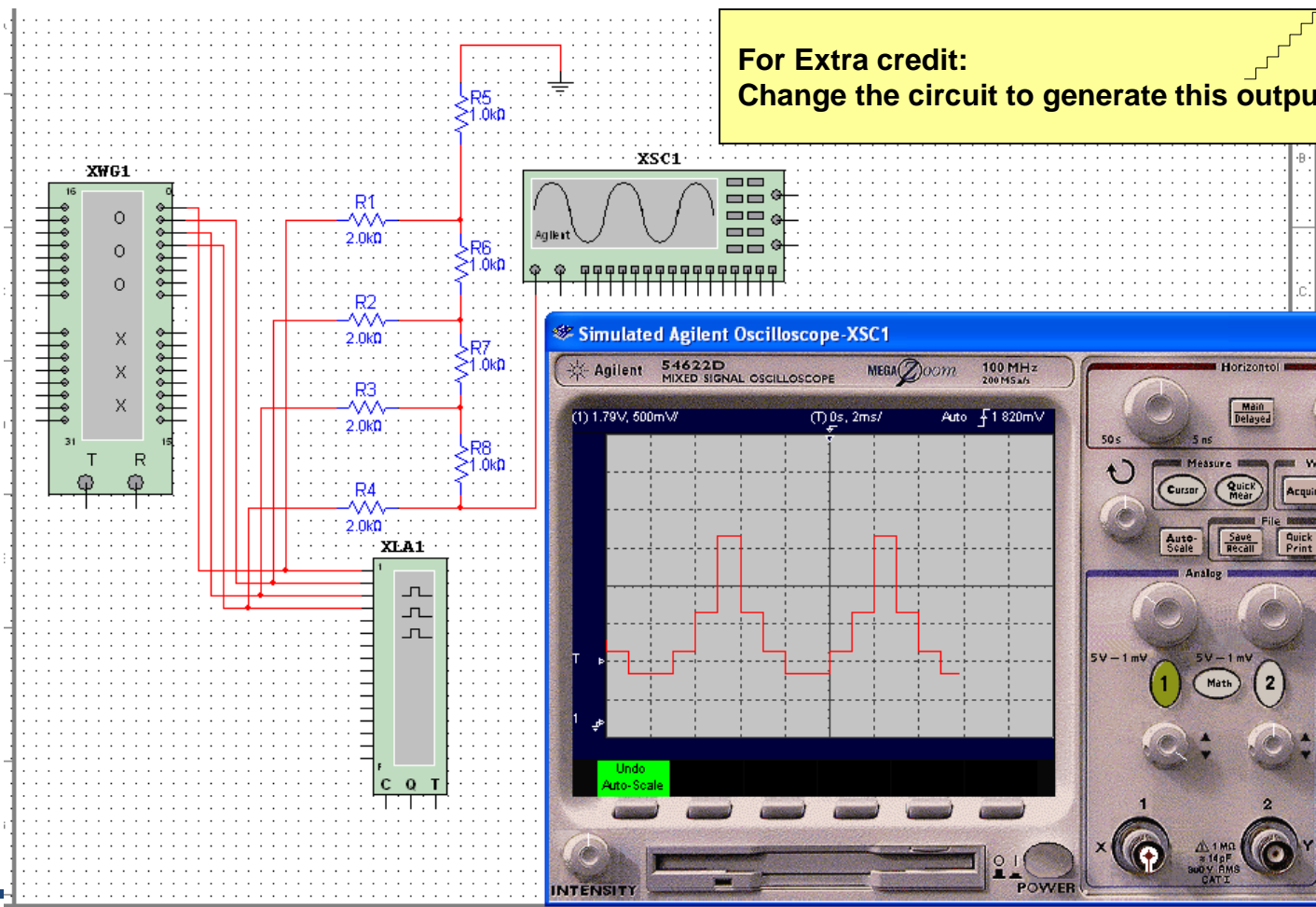
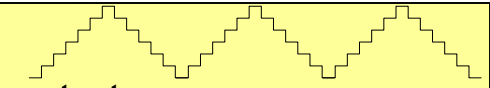
Only Input 3 is HIGH



Used for Digital-to-analog converter!

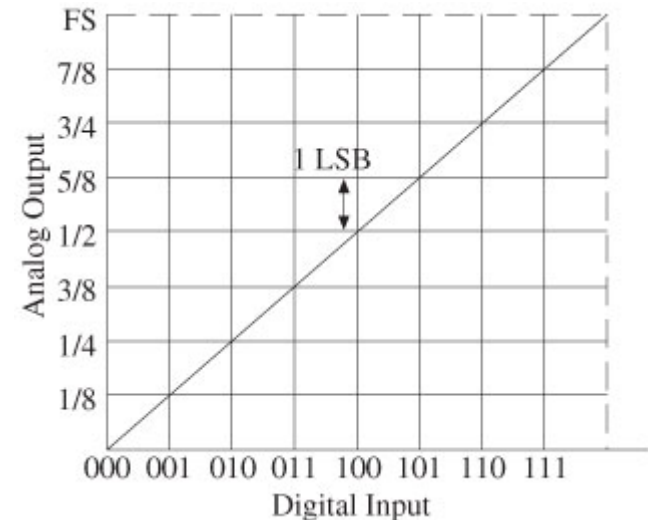
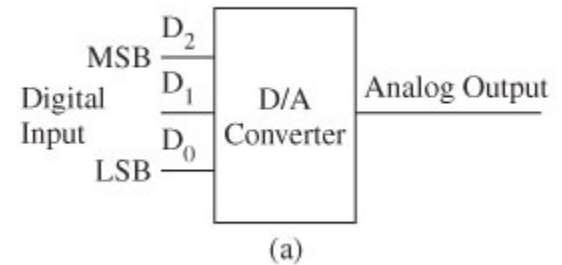
Examining Digital-to-Analog Conversion

For Extra credit:
Change the circuit to generate this output:



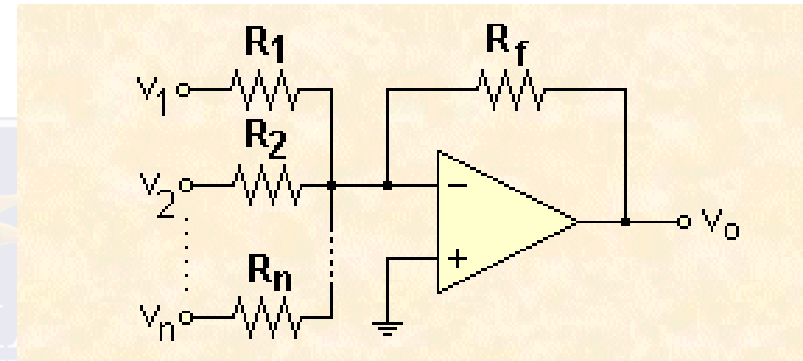
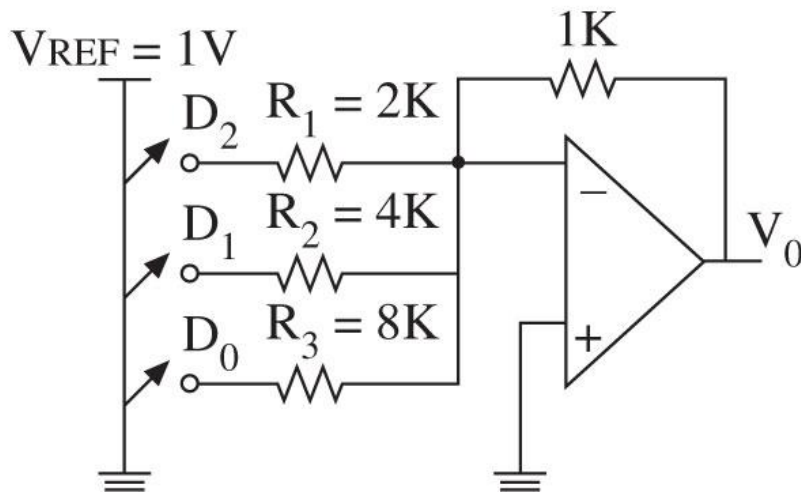
Digital to Analog Conversion

- The resolution of a DAC is defined in terms of **bits**—the same way as in ADC.
- The values of LSB, MSB, and full-scale voltages calculated the same way as in the ADC.
- The **largest** input signal 111 is equivalent of $7/8$ of the full-scale analog value.



- Can be designed using an operational amplifier and appropriate combination of resistors
- Resistors connected to data bits are in binary weighted proportion, and each is twice the value of the previous one.
- Each input signal can be connected to the op amp by turning on its switch to the reference voltage that represents logic 1.
 - If the switch is off, the input signal is logic 0.

- 3-bit D/A Converter Circuit



The transfer function of the summing amplifier :

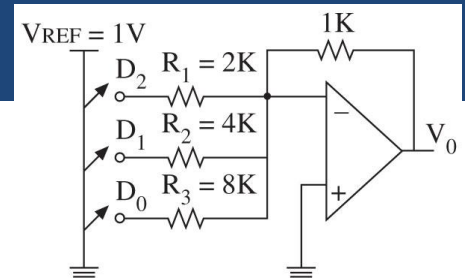
$$v_0 = -(v_1/R_1 + v_2/R_2 + \dots + v_n/R_n)R_f$$

Thus if all input resistors are equal, the output is a scaled sum of all inputs.

If they are different, the output is a **weighted** linear sum of all inputs.

Summing amplifier

- R/2R Ladder Network for D/A Converter



- If the reference voltage is 1 V, and if all switches are connected, the output current can be calculated as follows:

$$I_0 = I_T = I_1 + I_2 + I_3 = \frac{V_{REF}}{R_1} + \frac{V_{REF}}{R_2} + \frac{V_{REF}}{R_3} = \frac{V_{REF}}{1k} \left(\frac{1}{2} + \frac{1}{4} + \frac{1}{8} \right) = 0.875 \text{ mA}$$

- Output voltage

$$V_O = -R_f I_T = -(1k) \times (0.875 \text{ mA}) = -0.875 \text{ V} = \left| \frac{7}{8} \text{ V} \right|$$

D/A Converters as Integrated Circuits

- D/A converters are available commercially as integrated circuits
- Can be classified in **three categories**.
 - **Current output, voltage output, and multiplying type**
 - Current output DAC provides the current I_O as output signal
 - Voltage output D/A converts I_O into voltage internally by using an op amp and provides the **voltage** as output signal
 - In multiplying DAC, the output is **product** of the input voltage and the reference source V_{REF} .
 - Conceptually, all three types are similar

