$S M A_{t}=$ simple moving average at the end of the period $t$ or estimated demand at the end of that period.

$$
\mathrm{S} M A_{\mathrm{t}}=\frac{\mathrm{D}_{\mathrm{t}-(\mathrm{n}-1)}+\mathrm{D}_{\mathrm{t}-(\mathrm{n}-2)}+\ldots+\mathrm{D}_{\mathrm{t}-1}+\mathrm{D}_{\mathrm{t}}}{\mathrm{n}}
$$

3-month Simple Moving Average

| MONTH | ORDERS MONTH PER MONTH | $\begin{aligned} & \text { MOVING } \\ & \text { AVERAGE } \end{aligned}$ | $M A_{3}=$ |
| :---: | :---: | :---: | :---: |
| Jan | 120 | - | $\Gamma^{3}$ |
| Feb | 90 | - | $\sum_{i=1} D_{i} \quad 90+110+130$ |
| Mar | 100 | - | $\frac{i=1}{3}=\frac{}{3}=110$ |
| Apr | 75 | 103.3 | orders for Nov |
| May | 110 | 88.3 | orders for Nov |
| June | 50 | 95.0 |  |
| July | 75 | 78.3 |  |
| Aug | 130 | 78.3 |  |
| Sept | 110 | 85.0 |  |
| Oct | 90 | 105.0 |  |
| Nov | - | 110.0 |  |

5-month Simple Moving Average

| MONTH | ORDERS MONTH PER MONTH | MOVING <br> AVERAGE | $M A_{5}=$ |
| :---: | :---: | :---: | :---: |
| Jan | 120 | - |  |
| Feb | 90 | - | $\sum_{i=1} D_{i} \quad 90+110+130+75+50$ |
| Mar | 100 | - | $\frac{i=1}{3}=\frac{2}{5}=91$ |
| Apr | 75 | - | 5 orders for Nov |
| May | 110 | - | orders for Nov |
| June | 50 | 99.0 |  |
| July | 75 | 85.0 |  |
| Aug | 130 | 82.0 |  |
| Sept | 110 | 88.0 |  |
| Oct | 90 | 95.0 |  |
| Nov | - | 91.0 |  |

## Smoothing effects



Fig 3.1 Classification of production systems
Note: $\wedge$ It gives equal weight to the demand in each of the most $n$ periods.
人 Small value of n can capture data pattern more closely compared to high value of n Because high value of $n$ averages out more to the data or a greater smoothing effect on random fluctuations.

## Weighted Moving Average

While the moving average formula implies an equal weight being placed on each value that is being averaged, the weighted moving average permits an unequal weighting on prior time periods

$$
W M A_{t}=\sum_{i=1}^{n} W_{i} D_{i} \quad \sum_{\mathrm{i}=1}^{\mathrm{n}} \mathrm{w}_{\mathrm{i}}=1
$$

$\mathrm{w}_{\mathrm{t}}=$ weight given to time period " t " occurrence (weights must add to one)
th
Question: Given the weekly demand and weights, what is the forecast for the 4 period or Week 4 ?

| Week | Demand |
| ---: | ---: |
| 1 | 650 |
| 2 | 678 |
| 3 | 720 |
| 4 |  |


| Weights: |
| :--- |
| $\mathrm{t}-1$ |
| $\mathrm{t}-2$ |
| $\mathrm{t}-3$ |

Note that the weights place more emphasis on the most recent data, that is time period "t-1"

| Week | Demand | Forecast |
| ---: | ---: | ---: |
| 1 | 650 |  |
| 2 | 678 |  |
| 3 | 720 |  |
| 4 |  | 6934 |


| INPUT |
| :--- |
| - Material |
| - Machines |
| Labor |

## Exponential Smoothing

$$
F_{t+1}=\alpha D_{t}+(1-\alpha) F_{t}
$$

where:
$F_{t+1}=$ forecast for next period
$D_{t}=$ actual demand for present period
$F_{t}=$ previously determined forecast for present period
$\alpha=$ weighting factor, smoothing constant

## Effect of Smoothing Constant

$0.0 \leq \mathrm{a} \leq 1.0$
If $\mathrm{a}=0.20$, then $F_{t+1}=0.20 D_{t}+0.80 F_{t}$
If $\mathrm{a}=0$, then $F_{t+1}=0 D_{t}+1 F_{t}=F_{t}$
Forecast does not reflect recent data
If $\mathrm{a}=1$, then $F_{t+1}=1 D_{t}+0 F_{t}=D_{t}$
Forecast based only on most recent data

Question: Given the weekly demand data, what are the exponential smoothing forecasts for periods $10^{\text {th }}$ using $\mathrm{a}=0.10$ and $\mathrm{a}=0.60$ ?
Assume $\mathrm{F}_{1}=\mathrm{D}_{1}$

| Week | Demand |
| ---: | ---: |
| 1 | 820 |
| 2 | 775 |
| 3 | 680 |
| 4 | 655 |
| 5 | 750 |
| 6 | 802 |
| 7 | 798 |
| 8 | 689 |
| 9 | 775 |
| 10 |  |

Solution: The respective alphas columns denote the forecast values. Note that you can only forecast one time period into the future.

| Week | Demand | 0.1 | 0.6 |
| ---: | ---: | ---: | ---: |
| 1 | 820 | 820.00 | 820.00 |
| 2 | 775 | 820.00 | 820.00 |
| 3 | 680 | 815.50 | 793.00 |
| 4 | 655 | 801.95 | 725.20 |
| 5 | 750 | 787.26 | 683.08 |
| 6 | 802 | 783.53 | 723.23 |
| 7 | 798 | 785.38 | 770.49 |
| 8 | 689 | 786.64 | 787.00 |
| 9 | 775 | 776.88 | 728.20 |
| 10 |  | 776.69 | 756.28 |

Note how that the smaller alpha results in a smoother line in this example


Fig 3.2 Effect of Smoothing Constant

