Computer numbering systems

5.1 Binary numbers

The system of numbers in everyday use is the **denary** or **decimal** system of numbers, using the digits 0 to 9. It has ten different digits (0, 1, 2, 3, 4, 5, 6, 7, 8 and 9) and is said to have a **radix** or **base** of 10.

The **binary** system of numbers has a radix of 2 and uses only the digits 0 and 1.

5.2 Conversion of binary to denary

The denary number 234.5 is equivalent to

 $2 \times 10^{2} + 3 \times 10^{1} + 4 \times 10^{0} + 5 \times 10^{-1}$

i.e. is the sum of terms comprising: (a digit) multiplied by (the base raised to some power).

In the binary system of numbers, the base is 2, so 1101.1 is equivalent to:

 $1 \times 2^3 + 1 \times 2^2 + 0 \times 2^1 + 1 \times 2^0 + 1 \times 2^{-1}$

Thus the denary number equivalent to the binary number 1101.1 is

$$8 + 4 + 0 + 1 + \frac{1}{2}$$
, that is 13.5

i.e. $1101.1_2 = 13.5_{10}$, the suffixes 2 and 10 denoting binary and denary systems of numbers respectively.

Problem 1. Convert 11011_2 to a denary number.

From above: $11011_2 = 1 \times 2^4 + 1 \times 2^3 + 0 \times 2^2$ + $1 \times 2^1 + 1 \times 2^0$ = 16 + 8 + 0 + 2 + 1= 27_{10} *Problem 2.* Convert 0.1011₂ to a decimal fraction.

$$1011_{2} = 1 \times 2^{-1} + 0 \times 2^{-2} + 1 \times 2^{-3} + 1 \times 2^{-4}$$

= $1 \times \frac{1}{2} + 0 \times \frac{1}{2^{2}} + 1 \times \frac{1}{2^{3}} + 1 \times \frac{1}{2^{4}}$
= $\frac{1}{2} + \frac{1}{8} + \frac{1}{16}$
= $0.5 + 0.125 + 0.0625$
= 0.6875_{10}

Problem 3. Convert 101.0101₂ to a denary number.

$$101.0101_{2} = 1 \times 2^{2} + 0 \times 2^{1} + 1 \times 2^{0} + 0 \times 2^{-1}$$
$$+ 1 \times 2^{-2} + 0 \times 2^{-3} + 1 \times 2^{-4}$$
$$= 4 + 0 + 1 + 0 + 0.25 + 0 + 0.0625$$
$$= 5.3125_{10}$$

Now try the following exercise

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Exercise 17 Further problems on conversion of
binary to denary numbers (Answers
on page 272)
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In Problems 1 to 4, convert the binary numbers given to denary numbers.

1. (a) 110 (b) 1011 (c) 1110 (d) 1001

2. (a) 10101 (b) 11001 (c) 101101 (d) 110011