

Derivation

- ▶ Now, In this case our d_1 will be the distance between intersection point x and pixel x_k

$$d_1 = x - x_k \quad \text{By using(7)}$$

$$d_1 = 1/m(y_{k+1}-c) - x_k$$

And similarly our d_2 will be the distance between intersection point x and

- ▶ pixel x_{k+1}

$$d_2 = x_{k+1} - x \quad \text{By using(7)}$$

$$d_2 = x_{k+1} - 1/m(y_{k+1}-c)$$

- ▶ Note: here y is always incrementing so we can write y_{k+1} as y_k+1 and here x_{k+1} is next pixel so we can write it as x_k+1 .

subtracting d_2 from d_1

$$d_1 - d_2 = 1/m(y_k+1-c) - x_k - [x_k+1 - 1/m(y_k+1-c)]$$

$$= 1/m(y_k+1-c) - x_k - x_k - 1 + 1/m(y_k+1-c)$$

$$d_1 - d_2 = 2/m(y_k+1-c) - 2x_k - 1$$

$$d_1 - d_2 = 2dx(y_k+1-c) - 2dyx_k - dy$$

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- ▶ Multiplying both side by (dy)

$$dy(d_1-d_2) = 2dxy_k+2dx-2dxc-2dyx_k-dy$$

- ▶ Now we need to find decision parameter P_k

$$P_k = dy(d_1-d_2)$$

$$C = 2dx-2dxc-dy \text{ which is constant}$$

So new equation is

$$P_k = 2dxy_k-2dyx_k +C \text{(8)}$$

- ▶ Now our next parameter will be

$$P_{k+1} = 2dx(y_{k+1})-2dy(x_{k+1})+C$$

- ▶ Subtracting P_k from P_{k+1}

$$P_{k+1}-P_k = 2dx(y_{k+1}-y_k)-2dy(x_{k+1}-x_k)+C-C$$

Note: here x is always incrementing so we can write y_{k+1} as $y_k + 1$

$$P_{k+1}-P_k = 2dx(y_k + 1 - y_k) - 2dy(x_{k+1} - x_k)$$

$$P_{k+1} = P_k + 2dx - 2dy(x_{k+1} - x_k)$$

$$\text{when } P_k < 0 \text{ then } (d_1 - d_2) < 0$$

Derivation

- ▶ So $d_1 < d_2$ then we will write x_{k+1} as x_k because current pixel's distance from intersection point x is smaller. so, we will have to choose current pixel.

Then our formula will be:

$$P_{k+1} = P_k + 2dx - 2dy(x_k - x_k)$$

$$P_{k+1} = P_k + 2dx$$

And when $P_k > 0$ then $(d_1 - d_2) > 0$

- ▶ So $d_1 > d_2$ then we will write x_{k+1} as $x_k + 1$ because current pixel's distance from intersection point x is Larger. so, we will have to choose next pixel.

- ▶ At that time our formula will be:

$$P_{k+1} = P_k + 2dx - 2dy(x_k + 1 - x_k)$$

$$P_{k+1} = P_k + 2dx - 2dy$$

Derivation

- ▶ For Initial decision parameter

From 8th equation

$$P_k = 2dxy_k - 2dyx_k + C$$

$$P_0 = 2dxy_0 + 2dx - 2dxc - 2dyx_0 - dy$$

By using 1st equation

$$y_k = m(x_k) + c$$

- ▶ $c = y_k - m(x_k)$
 $P_0 = 2dxy_0 - 2dyx_0 + 2dx - 2dx(y_0 - m(x_0)) - dy$
 $P_0 = 2dxy_0 - 2dyx_0 + 2dx - 2dxy_0 + 2dyx_0 - dy$ (By using 2)
 $P_0 = 2dx - dy$

hence formulas for bresenham is derived.

Bresenham's Line Drawing Algorithm

Bresenham's Line Drawing Algorithm

```
#include<stdio.h>
#include<conio.h>
#include<graphics.h>
```

```
void main()
```

```
{
int gd =DETECT,gm;
initgraph(&gd,&gm,"C:\\\\TurboC3\\\\BGI");
int x,x1,y,y1,dx,dy,pk;
printf("Enter first co-ordinates");
scanf(" %d%d",&x,&y);
printf("Enter second co-ordinates");
scanf(" %d%d",&x1,&y1);
dx=x1-x;
dy=y1-y;
pk=2*dy-dx;
```

```
while(x<x1)
{ x++;
if(pk<0){
pk+=2*dy;
}
else{y++;
pk+=2*(dy-dx);
}
putpixel(x,y,9);
}
getch();
closegraph();

}
```