

Lecture No 43 Topic: Solution of Ordinary Differential Equations



A solution to the differential equation :

$$\ddot{x}(t) + 3\dot{x}(t) + 3x(t) = 0$$

$$\dot{x}(0) = 1; x(0) = 0$$

is a function $x(t)$ that satisfies the equations.

- * Analytical solutions are available for special cases only.

Solution of Partial Differential Equations

Partial Differential Equations are more difficult to solve than ordinary differential equations:

$$\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial t^2} + 2 = 0$$

$$u(0, t) = u(1, t) = 0, u(x, 0) = \sin(\pi x)$$

Questions

1. Find the positive root of $x^4 - x = 10$ correct to three decimal places using Newton – Raphson method.
2. Using Newton iterative method find the root between 0 & 1 of $x^3 = 6x - 4$ correct to two places.
3. Find the real positive root of $3x - \cos x - 1 = 0$ by newton method coprrect to 6 decimal places.
4. Find a root of $x \log_{10} x - 1.2 = 0$ by N – R method correct to 3 decimal places.
5. Obtain newton iterative formula for finding root N . where N is a positive real number. Hence evaluate root of 142.
6. Solve the following system of equations by Gauss – Jordon method.
 $10x + y + z = 12$, $2x + 10y + z = 13$, $x + y + 5z = 7$